

## *More Detailed List of Topics*

### **Linear Equations in Linear Algebra**

Systems of Linear Equations  
Row Reduction and Echelon Forms  
Vector Equations  
The Matrix Equation  $\mathbf{Ax} = \mathbf{b}$   
Solution Sets of Linear Systems  
Applications of Linear Systems  
Linear Independence  
Introduction to Linear Transformations  
The Matrix of a Linear Transformation  
Linear Models in Business, Science, and Engineering

### **Matrix Algebra**

Matrix Operations  
The Inverse of a Matrix  
Characterizations of Invertible Matrices  
Partitioned Matrices  
Matrix Factorizations  
The Leontief Input—Output Model  
Applications to Computer Graphics  
Subspaces of  $\mathbb{R}^n$   
Dimension and Rank

### **Vector Spaces**

Vector Spaces and Subspaces  
Null Spaces, Column Spaces, and Linear Transformations  
Linearly Independent Sets; Bases  
Coordinate Systems  
The Dimension of a Vector Space  
Rank; Change of Basis  
Applications to Markov Chains

### **Eigenvalues and Eigenvectors**

Eigenvectors and Eigenvalues  
The Characteristic Equation  
Diagonalization  
Eigenvectors and Linear Transformations

### **Determinants**

Introduction to Determinants  
Properties of Determinants

### **Finite-State Markov Chains**

Google and Markov Chains  
The Steady-State Vector and Google's PageRank

### **Orthogonality and Least Squares**

Inner Product, Length, and Orthogonality  
Orthogonal Sets  
Orthogonal Projections  
The Gram—Schmidt Process  
Least-Squares Problems