

Multivariable Calculus: A Linear Algebra Approach

Errata and Additions

February 9, 2026

Preface: Page xiii, last line: " Duncan McCabe, an undergraduate mathematics major at Middlebury, " should be "Duncan McCabe and Cody Matice, undergraduate mathematics majors at Middlebury, "

Chapter 1: Page 11: "We will usually write $-(x)$ " should be "We will usually write $-x$ "

Page 15, line 6: Delete **Invertibility**

Page 15, 3 lines from bottom replace " $+c_3$ " with " $+c_3 - c_4$ "

Page 17: Add Section on Mathematical Induction

Chapter 2: Page 28, Example 2: "8 f/sec" should be "8 ft/sec"

Page 31: " $(kg)^{-2}$ " should be " $(\text{kg})^{-2}$ "

Page 34: In all of the equations replace lower case e with upper case E.

Page 41: Project 1: insert right parenthesis between βt and $0 \leq t$

Chapter 3

Page 44, line 2: "An individual" should be "If an individual"

Page 47, Example 2: f_x should be f_x , f_y should be f_y and f_z should be f_z .

Page 48, **Alternative Notation** replace "notation $\frac{\partial f}{\partial x}$ " with "notation $\frac{\partial^2 f}{\partial x^2} = \frac{\partial}{\partial x} \left(\frac{\partial f}{\partial x} \right)$ "

Page 57: Second **Example 2** should be **Example 3**

Page 58: **Example 3** should be **Example 4**. Also " $\$D$ " should be " $\$D$ "

Page 58, 6 lines from bottom: Add colon (:) after **Solution**

Page 60, Exercise 20: " let " should be " Let "

Chapter 3: Page 62 , Exercise 7: Line 1: $(x_4, x_5, 6)$ should be (x_4, x_5, x_6) .

Line 2: Replace existing text with. following:

(a) Determine $f(10, 23, 18, 12, 30, 21)$.

(b) Describe the set of points (x, y, z) in space such that $f(1, 1, 1, x, y, z) = 0$.

Chapter 4: Page 70: Line 6 of **Proof of (d)**: $\mathcal{M}_2, \mathcal{M}_2$ should be $\mathcal{M}_1, \mathcal{M}_2$

Page 71, Example 2:: $\cos xe^y$ should be $\cos x + e^y$

Page 81, 3rd line of Example 3: Change "length of \mathbf{v} =" to "length of \mathbf{v} . which is "

Page 84, Line 2: delete period in "joining them as."

Page 86, Second line of Section 4.6: $-1 \leq \cos \theta \leq 1$ should be $-1 \leq \cos \theta \leq 1$

Page 89, Second Line of 4.6.2 Newton's Method: $x - 2 = 0$ should be $x^2 - 2 = 0$

Page 96, Exercise 17: Delete left parenthesis (from "for $(x \neq 0$

Page 98, Line 2: right after "vector - valued functions", add "in Exercises 30 - 32"

Page 99, Exercise 39: Change "1,00,000" to "1,000,000"

Chapter 5 : **Need to Number the Theorems.**

Page 101: First Line of 5.1.1: Change " **Theorem: The Little Chain Rule** " to " **Theorem 5.1.1 (The Little Chain Rule)** :"

Page 103: First Line of 5.1.2: Change " **Theorem: General Chain Rule** " to " **Theorem 5.1.2 (General Chain Rule)** :"

Page 104, Line 1: Insert colon (:) immediately after **Solution**

Page 107, second line after "so": $= 9f(u)^2 + 12f_u^* f_v^* + 4(f_v^*)^2 + 4f(u)^2 - 12f_u^* f_v^* + 9f(v)^2$
 should be $= 9(f_u^*)^2 + 12f_u^* f_v^* + 4(f_v^*)^2 + 4(f_u^*)^2 - 12f_u^* f_v^* + 9(f_v^*)^2$

Page 109, Line 7 in Section 5.3: " $\frac{\partial f}{\partial x_1} \frac{\partial f}{\partial x_2}$ " should be " $\frac{\partial f}{\partial x_1}, \frac{\partial f}{\partial x_2}$ "

Page 110: 4th line in Example 3: "The text " should be "The test "

Page 113: In paragraph "Let's look a bit": Change "differentiable function real-valued" to "differentiable real-valued"

Page 121, Example 11: Both instances of "\$C" should be "\$C"

Page 121, 2 line from bottom: " $3xx$ " should be " $3x$ "

Page 124, First Definition: "*Hessian Matrix*" should be "**Hessian Matrix**"

Page 124, Second Definition: "*Positive-Definite Matrix*" should be "**Positive-Definite Matrix**" and "*positive semi-definite*" should be "**positive semi-definite**"

Page 129, in Example 2, change "You can" to "We can "

Page 131, Sentence beginning "Figure 5/17 illustrates ": insert period at end of sentence.

Page 139, Exercise 37. Delete period (.) in first line.

Page 139, Exercise 42, last line: Add right parenthesis so $(\mathbf{c}, f(\mathbf{c}))$ becomes $(\mathbf{c}, f(\mathbf{c}))$

Page 139, Exercise 48: add:

(a): Show that $f(x, y) = 4x^2 + 8xy + 5y^2$ is a positive-definite function.

(b) Show that $g(x, y) = -x^2 + 2xy - 3y^2$ is a negative-definite function

Page 141, Exercise 63: Change "\$T" to "\$T"

Page 142, Exercise 64: Change "\$p" to "\$p", "\$q" to "\$q", and "\$B" to "\$B"

Page 142, Exercise 65: Change "\$C" to "\$C"

Chapter 6

Page 158: italicize x in **x-simple** and the y in **y-simple**

Page 160, 7 lines from bottom: delete period in "such that."

Page 161, 8 lines from bottom: "with mesh less than " should be "with mesh less than "

Page 162, **Proof of (2)**: Change "use" to "Use"

Page 163, Line 7: Insert line break just before **Partition Theorem**

Page 167, Line 3; Insert equality sign (=) between $\frac{1}{2}(u-1)^{-1}$ and $\frac{1}{2\sqrt{u-1}}$.

Page 174, Line 3 of **Solution**: Add colon after *Method A*

Page 175, 8 lines from bottom: "as $as \rightarrow 0$ " should be "as $a \rightarrow 0$ "

Page 175, 3 lines from bottom " $\int_D f DA$ " should be " $\int_D f dA$ "

Page 182, Exercise 8: " $x - axis$ " should be " x -axis "

Page 185, Exercise 32: Add at the start: "Determine the convergence or divergence of the integral"

Page 185,k Exercise 35b: Formula at end of the line should read

$$\frac{1}{\lambda} [\lambda^2 - 1 + e^{-3\lambda}(11 + 3\lambda)]$$

Chapter 7:

Page 191, About 5 lines from bottom: Equation with *Work* =: "Work" should not be italicized

Page 196, 9 lines from bottom: " $0 \leq s11$ " should be " $0 \leq s \leq 1$ "

Page 201, 4th line in Solution of Example 6: " \cos^t " should be " $\cos^2 t$ "

Page 201, 8th line in Solution of Example 6: $\mathcal{L}(\gamma) = \int_0^{\pi/2} \int |\mathbf{g}'(t)| dt =$ should be $\mathcal{L}(\gamma) = \int_0^{\pi/2} |\mathbf{g}'(t)| dt =$

Page 201, 11th line in Solution of Example 6: $\mathcal{L}(\gamma) = \int_0^{\pi/2} \int |\mathbf{g}'(t)| dt =$ should be $\mathcal{L}(\gamma) = \int_0^{\pi/2} |\mathbf{g}'(t)| dt =$

Page 202, Example 7: " 4π " should be " 4π "

Page 205, 7 lines from bottom: "straight forward" should be "straightforward"

Page 211, 2nd line of proof of Theorem 6.2: " $\mathbf{T}' = \frac{d\mathbf{T}}{t}$ " should be " $\mathbf{T}' = \frac{d\mathbf{T}}{dt}$ "

Page 220, Exercise 12: " $2xx^2$ " should be " $2x^2$ "

Page 220, Exercise 14: " \mathbf{g} " should be " $\mathbf{g}(t)$ "

Page 220, Exercise 15: " $\mathbf{h}s$ " should be " $\mathbf{h}(t)$ "

Page 222, Exercise 26: " \cosh " should be " \sinh "

Page 222, Exercise 28: " **y-axis** " should be " y -axis "

Page 222, Exercise 30: Sketch the solid obtained by revolving the graph of $y = 4\sqrt[3]{x}$ from (8,8) to (27, 12) around the y -axis and determine its surface area.

Page 223, Replace Exercise 41 of Chapter. 7 with:

For each of the following, sketch the curve with the given equation and determine its curvature:

(a) $y = x^2$

(b) $y = x^3$

(c) $y = x^4$

(d) $y = x^5$

(e) $y = x^{-1}, x > 0$

(f) $y = x^{-2}, x > 0$

(g) $y = \ln x, x > 0$

Page 224, Exercise 48(b): " $-\frac{2A}{5}$ " should be " $\frac{2A}{5}$ "

Page 224, Exercise 49: " $7x$ " should be " $-7x$ "

Page 224, Exercise 50: " $-x + 3y$ " should be " $4x + y$ "

Page 225, Exercise 55(e): " $v_1v_2V_2$ " should be " $v_1v_2v_3$ "

Page 226, **Art Gallery Problem**: " $\lfloor 3 \rfloor = \lfloor 4 \rfloor = \lfloor 5 \rfloor = 1$, but $\lfloor 6 \rfloor = 2$. " should be " $\lfloor 3/3 \rfloor = \lfloor 4/3 \rfloor = \lfloor 5/3 \rfloor = 1$, but $\lfloor 6/3 \rfloor = 2$. "

Page 230, Add colon after **Example 3**

Chapter 8:

Page 229, 2nd line from bottom: "For points above this line, $\operatorname{div} \mathbf{F}$ is positive " should be "For points below this line, $\operatorname{div} \mathbf{F}$ is positive "

Page 248: Line. 1: " X^2 " should be " x_2 "

Page 258, 9 lines from bottom: " $dx dy dx$ " should be " $dx dy dz$ "

Page 276. Exercise 21. (a) and (b): " $-\leq t$ " should be " $0 \leq t$ "

Page 275, Exercise 5: " $m \times n$ " should be " $n \times n$ "

Page 276, Exercise 18: " $(y + 2x, x + 3x, 2x + 3y)$ " should be " $(y + 2x, x + 3z, 2z + 3y)$ "

Page 276, Exercise 21(a) and (b) " $-\leq t$ " should be " $0 \leq t$ "

Page 277, Exercise 29(d), 3rd line: " $g(\sigma(S, t))$ " should be " $f(\sigma(s, t))$ "

Page 277, Exercise 31: The vector field should be $\mathbf{F}(x, y, z) = (x, 2y, 3z)$.

Chapter 9:

Page 290, Line 2: " *partialR* " should be " ∂R "

Page 291, Exercises 3, 4, 5: " *gamma* " should be " γ "

Chapter 9:

Page 290, 2nd line of Proof of Theorem: The dash (-) should be an equal sign (=)

Page 291: Replace Exercises 1 - 5 with:

1. Find $\int_{\gamma} \omega$ if $\omega = \frac{-y}{x^2+y^2} dx + \frac{x}{x^2+y^2} dy$ and γ is the circle of radius 2, centered at the origin and traced out counterclockwise.
2. Find $\int_{\gamma} \omega$ if $\omega = x dx + dy$ and γ the graph of $\frac{x^2}{9} + \frac{y^2}{4} = 1$ traced out counterclockwise.
3. Find $\int_{\gamma} \omega$ if $\omega = y dx + x dy$ and γ has the parametrization $g(t) = (\cos t, \sin t, t), 0 \leq t \leq 2\pi$.
4. Find $\int_{\gamma} \omega$ if $\omega = (x+y) dx + zy^2 dy + (x-z) dz$ and γ in the line segment from (1, 2, 3) to (4, -3, 7).
5. Find $\int_{\gamma} \omega$ if $\omega = (x^2 + yz) dx + z dy + (y-x) dz$ and γ has parametrization $g(t) = (2t+3, 3t-2, t+4), 0 \leq t \leq 2$.

IF POSSIBLE, ADD THE FOLLOWING AT END OF SECTION 1.2.4 BEFORE SECTION 1.3:

Example: Suppose $\lambda \neq \mu$ are distinct eigenvalues of the matrix A with corresponding eigenvectors \mathbf{v} and \mathbf{u} . Thus \mathbf{v} and \mathbf{u} are nonzero vectors with $A\mathbf{v} = \lambda\mathbf{v}$ and $A\mathbf{u} = \mu\mathbf{u}$. Show that $\{\mathbf{v}, \mathbf{u}\}$ is a linearly independent set.

Solution: Suppose c and d are constants such that

$$(*) \quad c\mathbf{v} + d\mathbf{u} = \mathbf{0}.$$

We need to show that both c and d must be 0. Let's multiply both sides of (*) by the matrix A :

$$A(c\mathbf{v} + d\mathbf{u}) = A(c\mathbf{v}) + A(d\mathbf{u}) = cA\mathbf{v} + dA\mathbf{u} = c\lambda\mathbf{v} + d\mu\mathbf{u} = A\mathbf{0} = \mathbf{0}.$$

Thus we have

$$(**) \quad c\lambda\mathbf{v} + d\mu\mathbf{u} = \mathbf{0}.$$

If we multiply (*) by λ , we obtain

$$(***) \quad c\lambda\mathbf{v} + d\lambda\mathbf{u} = \mathbf{0}.$$

Subtract equation (***) from (**) to obtain

$$d(\mu - \lambda)\mathbf{u} = \mathbf{0},$$

but $\mu - \lambda$ is a nonzero number since the eigenvalues are distinct. Hence $d\mathbf{u} = \mathbf{0}$ which implies $d = 0$ because \mathbf{u} is a nonzero vector. Equation (*) reduces to $c\mathbf{v} = \mathbf{0}$ which also implies $c = 0$ by the nonzero character of the vector \mathbf{v} .

Add a New Exercise 24 for Chapter 1:

Exercise: Let $\lambda_1, \lambda_2, \lambda_3$ be three distinct eigenvalues of the same matrix A with corresponding eigenvectors $\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3$. Prove that the set of these eigenvectors is linearly independent.